Course Title: $\quad 7^{\text {th }}$ Grade Math
Board Approval Date: 6/2018
Credit / Hours:
Reviewed Annually

## Course Description:

Seventh grade math focuses on mastery of the PA Academic Standards for $7^{\text {th }}$ grade math and incorporates the Assessment Anchors and Eligible Content. As students progress through this course, they will learn operations on rational numbers, expressions and equations, inequalities, proportional relationships, percents, angles and triangles, plane geometry and similarity, surface area, volume, data and statistics, and probability. Integrated into every unit are rigorous, real-world applications of the standards.

## Learming Activines / IVIodes ol Assessmieni:

Direct Instruction
Guided Notes
Cooperative/Small Group Work
Stations
Teacher Observations
Quizzes/Tests
AIMSWEB/CDTs

Instructional Resources:
Teacher made resources aligned to standards, eligible content, and assessment anchors.
Study Island
iXL
Other various applications

Course Pacing Guide<br>$7^{\text {th }}$ Grade Math

Unit Name
Unit 1 Rational Numbers ..... 20
Unit 2 Expressions and Equations ..... 20
Unit 3 Inequalities ..... 12
Unit 4 Proportional Relationships ..... 30
Unit 5 Percents ..... 15
Unit 6 Angles and Triangles ..... 20
Unit 7 Plane Geometry and Similarity ..... 20
Unit 8 Surface Area ..... 10
Unit 9 Volume ..... 10
Unit 10 Data and Statistics ..... 10
Unit 11 Probability ..... 10
177 days

Topic: Unit 1: Rational Numbers
Days: 20
Subject(s): $7^{\text {th }}$ Grade Math

| Know: | Understand: | Do: |
| :---: | :---: | :---: |
| Absolute Value <br> Difference <br> Integer <br> Natural Number <br> Numerical Expression <br> Product <br> Opposite <br> Quotient <br> Rational Number <br> Reciprocal <br> Sum <br> Whole Number | Understanding add and subtract rational numbers. <br> Understand situations in which opposites combine to make zero. <br> Understand multiply and divide rational numbers. <br> Understand solving real-world and mathematical problems involving the four operations with rational numbers. | M07.A-N.1.1.1 Apply properties of operations to add and subtract rational numbers, including real-world situations. <br> M07.A-N.1.1.2 Represent addition and subtraction on a horizontal or vertical number line. <br> M07.A-N.1.1.3 Apply properties of operations to multiply and divide rational numbers, including real-world contexts; demonstrate that the decimal form of a rational number terminates or eventually repeats. <br> M07.B-E.2.1.1 Apply properties of operations to calculate with numbers in any form; convert between forms as appropriate. |

Topic: Unit 2: Equations and Expressions
Days: 20
Subject(s): $7^{\text {th }}$ Grade Math

| Know: | Understand: | Do: |
| :---: | :---: | :---: |
| Algebraic Expressions <br> Associate Property <br> Coefficient <br> Commutative Property <br> Distributive Property <br> Equation <br> Equivalent <br> Evaluate <br> Expressions <br> Identity Property <br> Simplify <br> Variable | Understanding properties of operations as strategies to add, subtract, factor, and expand linear expressions with rational coefficients. <br> Understand solving multi-step real-life and mathematical problems posed with positive and negative rational numbers in any form (whole numbers, fractions, and decimals) <br> Understand using variables to represent quantities | M07.B-E.1.1.1 Use properties of operations to generate equivalent expressions. <br> M07.B-E.2.2.1 Use variables to represent quantities in a real-world or mathematical problem and construct simple equations and inequalities to solve problems. |

## Unit Essential Ouestion:

How do you perform operations on rational numbers?

| Concept: <br> Adding and Subtracting Integers | Concept: <br> Adding and Subtracting Rational Numbers | Concept: <br> Multiplying and Dividing Integers | Concept: <br> Multiplying and Dividing Rational Numbers |
| :---: | :---: | :---: | :---: |
| $\square$ |  |  |  |
| Lesson Essential Question/s: <br> How are numbers represented on a number line? <br> How do you add integers? <br> How do you subtract integers? | Lesson Essential Question/s: <br> How do you add rational numbers? <br> How do you subtract rational numbers? | Lesson Essential Question/s: <br> How do you multiply integers? <br> How do you divide integers? | Lesson Essential Ouestion/s: <br> How do you multiply rational numbers? <br> How do you divide rational numbers? |
| $\square$ |  |  |  |
| Vocabulary: <br> - Absolute Value <br> - Opposites <br> - Integer <br> - Natural Number <br> - Whole Number <br> - Sum <br> - Difference <br> - Numerical Expression | Vocabulary: <br> - Rational Number | Vocabulary: <br> - Product <br> - Quotient | Vocabulary: <br> - Reciprocal |

## Unit Essential Ouestion:

How do you simplify expressions and solve equations?

| Concept: <br> Expressions | Concept: <br> Equations | Concept: <br> Real-World <br> Applications | Concept: |
| :---: | :---: | :---: | :---: |
| $\sqrt{7}$ |  |  |  |
| Lesson Essential Question/s: <br> How do you combine like terms? <br> How do you simplify using the distributive property? <br> How do you factor an expression? | Lesson Essential Question/s: <br> How do you solve onestep equations? <br> How do you solve twostep equations? <br> How do you solve twostep equations with rational numbers? <br> How do you solve multi-step equations? | Lesson Essential Ouestion/s: <br> How do you write and solve equations to model real-life problems? | $\frac{\text { Lesson Essential }}{\text { Question/s: }}$ |
| $\square$ |  |  |  |
| Vocabulary: <br> - Expression <br> - Equivalent <br> - Like Terms <br> - Term <br> - Coefficient <br> - Constant Term <br> - Variable Term <br> - Simplify | Vocabulary: <br> - Evaluate | Vocabulary: | Vocabulary: |


| $\bullet$ | Distributive |  |  |
| :--- | :--- | :--- | :--- |
| Property <br> Factoring |  |  |  |

Course/Subject: $7^{\text {th }}$ Grade Math Length of instruction: 12 Days

Unit 3 Inequalities

## Unit Essential Ouestion:

How do you solve and graph inequalities?

| Concept: <br> Inequalities | Concept: | Concept: <br> Real-World <br> Applications | Concept: |
| :---: | :---: | :---: | :---: |
| $\sqrt{5}$ |  |  |  |
| Lesson Essential Question/s: <br> How do you solve and graph inequalities | Lesson Essential Question/s: | Lesson Essential Question/s: <br> How do you write and solve inequalities to model real-life problems? | Lesson Essential Question/s: |
| $\square$ |  |  |  |
| Vocabulary: <br> - Inequality <br> - Greater than <br> - Less than <br> - Greater than or equal to <br> - Less than or equal to | Vocabulary: | Vocabulary: | Vocabulary: |

Topic: Unit 3: Inequalities
Days: 12
Subject(s): $7^{\text {th }}$ Grade Math

| Know: | Understand: | Do: |
| :---: | :---: | :---: |
| Inequality <br> Greater than <br> Less than Greater than or equal to Less than or equal to | Understand how variables are used to represent quantities in real-world or mathematical problems, and construct simple equations and inequalities to solve problems by reasoning about the quantities. <br> Understand how to solve word problems leading to inequalities of the form $p x+q>r$ or $p x+q<r$, where $p$, $q$, and $r$ are specific rational numbers. Graph the solution set of the inequality and interpret it in the context of the problem. | M07.B-E.1.1.1 Use properties of operations to generate equivalent expressions. <br> M07.B-E.2.2.1 Use variables to represent quantities in a real-world or mathematical problem and construct simple equations and inequalities to solve problems. |

Topic: Unit 4: Proportional Relationships
Subject(s): $7^{\text {th }}$ Grade Math

| Know: | Understand: | Do: |
| :---: | :---: | :---: |
| Axis <br> Constant of Proportionality <br> Coordinate Grid <br> Dependent Variable <br> Independent Variable <br> Linear <br> Non-linear <br> Non-proportional <br> Ordered Pair <br> Origin <br> Proportional <br> Rate <br> Rate of Change <br> Unit Price <br> Unit Rate <br> X-axis <br> Y -axis | Understanding compare unit rates associated with ratios of fractions, including ratios of length, areas, and other quantities measured in like or different units <br> Understand recognize and represent proportional relationships between quantities. <br> Understand to analyze, recognize, and represent proportional relationships and use them to solve realworld and mathematical problems. | M07.A-R.1.1.1 Compute unit rates associated with ratios of fractions, including ratios of lengths, areas, and other quantities measured in like or different units. <br> M07.A-R.1.1.2 Determine whether two quantities are proportionally related (e.g. by testing for equivalent ratios in a table, graphing on a coordinate plane and observing whether the graph is a straight line through the origin). <br> M07.A-R.1.1.3 Identify the constant of proportionality (unit rate) in tables, equations, diagrams, and verbal descriptions of proportional relationships. <br> M07.A-R.1.1.4 Represent proportional relationships by equations. <br> M07.A-R.1.1.5 Explain what the point $(x, y)$ on the graph of a proportional relationship means in terms of the situation, with special attention to the points $(0,0)$ and $(1, r)$ where $r$ is the unit rate. <br> M07.A-R.1.1.6 Use proportional relationships to solve multi-step ratio and percent problems. |

## Unit Essential Ouestion:

How do you represent proportional relationships?

| Concept: <br> Constant of Proportionality | Concept: <br> Proportional Relationships | Concept: <br> Unit Rates | Concept: |
| :---: | :---: | :---: | :---: |
| $\sqrt{5}$ |  |  |  |
| Lesson Essential Question/s: <br> How do you find and apply the constant of proportionality? | Lesson Essential Question/s: <br> How do you represent a proportional relationship in a table? <br> How do you represent a proportional relationship in a graph? <br> How do you represent a proportional relationship in an equation? | Lesson Essential Question/s: <br> How do you find and apply unit rates in proportional relationships? | $\frac{\text { Lesson Essential }}{\text { Ouestion/s: }}$ |
| $\square$ |  |  |  |
| Vocabulary: <br> - Constant of Proportionality <br> - Proportional | Vocabulary: <br> - Axis <br> - Coordinate Grid <br> - Dependent Variable <br> - Independent Variable <br> - Linear <br> - Non-linear | Vocabulary: <br> - Rate <br> - Rate of Change <br> - Unit Price <br> - Unit Rate | Vocabulary: |


|  | $\bullet$ Non- |  |  |
| :--- | :--- | :--- | :--- | :--- |
|  | proportional  <br> $\bullet$ Ordered Pair <br> $\bullet$  <br>  $\bullet$ Origin <br>   <br>  x-axis <br>   <br>  y-axis |  |  |

## Unit Essential Ouestion:

How do you solve problems involving percents?


|  | $\bullet$ | Simple |  |  |
| :--- | :--- | :--- | :--- | :--- |
|  | Interest |  |  |  |
|  | $\bullet$ | Tip |  |  |
|  | $\bullet$ (Gratuity) |  |  |  |

Topic: Unit 5: Percents
Days: 15
Subject(s): $7^{\text {th }}$ Grade Math

| Know: | Understand: | Do: |
| :---: | :---: | :---: |
| Commission <br> Mark Down <br> Mark Up <br> Percent <br> Percent Change <br> Percent Equation <br> Percent Decrease <br> Percent Increase <br> Percent Proportion <br> Proportion <br> Sales Tax <br> Simple Interest <br> Tip (Gratuity) <br> Unit Rate | Understand how a percent is a part of a whole (total) and apply that to a variety of multi-step percent problems. <br> Understand how to use proportional relationships to solve multistep ratio and percent problems. <br> Understand how to recognize and represent proportional relationships between quantities. | M07.B-E.2.1.1 Apply properties of operations to calculate with numbers in any form; convert between forms as appropriate. <br> M07.A-R.1.1.6 Use proportional relationships to solve multi-step ratio and percent problems. |

Topic: Unit 6: Angles \& Triangles
Days: 20
Subject(s): $7^{\text {th }}$ Grade Math


## Unit Essential Ouestion:

How are angles and triangles related?

| Concept: <br> Angle Relationships | Concept: <br> Triangles | Concept: | Concept: |
| :---: | :---: | :---: | :---: |
| $\square$ |  | $\square$ | $\square$ |
| Lesson Essential Question/s: <br> How are complementary and supplementary angles related? <br> How are vertical and adjacent angles related? <br> How are angles related when two parallel lines are cut by a transversal? | Lesson Essential Question/s: <br> How are angles in a triangle related? <br> How are sides in a triangle related? <br> How do you use and apply the Triangle Inequality Theorem? | Lesson Essential Question/s: | Lesson Essential Question/s: |
| $\square$ - |  |  |  |
| Vocabulary: <br> - Acute Angle <br> - Adjacent Angles <br> - Alternate Exterior Angles <br> - Alternate Interior Angles <br> - Complementary Angle <br> - Congruent <br> - Corresponding | Vocabularv: <br> - Acute Triangle <br> - Isosceles Triangle <br> - Obtuse Triangle <br> - Right Triangle <br> - Scalene Triangle <br> - Triangle Inequality Theorem <br> - Vertex | Vocabularv: | Vocabularv: |

- Obtuse Angle
- Parallel Lines
- Right Angle
- Straight Angle
- Supplementary
- Transversal
- Vertical Angles
- Equilateral

Triangle

Topic: Unit 7: Plane Geometry and Similarity
Days: 20
Subject(s): $7^{\text {th }}$ Grade Math

| Know: | Understand: | Do: |
| :---: | :---: | :---: |
| Circle <br> Circumference <br> Cube <br> Cylinder | Understand how to solve problems involving scale drawings of geometric figures. | M07.C-G.1.1.1 Solve problems involving scale drawing of geometric figures, including finding length and area. <br> M07.C-G.1.1.4 Describe the two-dimensional figures that result from slicing threedimensional figures. |
| Diameter Edge | Understand the formulas for the area and circumference of a circle and use them | M07.C-G.2.2.1 Find the area and circumference of a circle. Solve problems involving area and circumference of a circle(s). |
| Face <br> Irregular Polygon | to solve problems. | M07.C-G.2.2.2 Solve real-world and mathematical problems involving area, |
| Leg Net | Understand how to solve real-world mathematical problems involving | dimensional objects composed of triangles, quadrilaterals, polygons, cubes, and right prisms. |
| Prism | surface area of two- |  |
| Pyramid | and three-dimensional objects composted of |  |
| Radius | triangles, quadrilaterals, |  |
| Rectangular Prism | polygons, cubes, and right prisms. |  |
| Regular Polygon |  |  |
| Scale Drawing |  |  |
| Scale Factor |  |  |
| Similar |  |  |
| Surface Area |  |  |

Topic: Unit 8: Surface Area
Days: 10
Subject(s): $7^{\text {th }}$ Grade Math

| Know: | Understand: |  |
| :--- | :--- | :--- |
| Cube | Understand how to <br> solve real-world <br> mathematical <br> problems involving <br> area, volume, and <br> surface area of two- <br> and three-dimensional <br> objects composted of <br> triangles, <br> quadrilaterals, <br> polygons, cubes, and <br> right prisms. | M07.C-G.2.2.2 Solve real-world and <br> mathematical problems involving area, <br> volume, and surface area of two- and three- <br> dimensional objects composed of triangles, <br> quadrilaterals, polygons, cubes, and right <br> prisms. |
| Net |  |  |
| Prism |  |  |
| Pyramid |  |  |
| Rectangular Prism |  |  |
| Rurface Area |  |  |

Course/Subject: $7^{\text {th }}$ Grade Math Length of instruction: 20 Days
Unit 7 Plane Geometry and Similarity

## Unit Essential Ouestion:

How do you find the area of plane geometric figures?

How are similar figures and scale drawings related?

| Concept: <br> Circles | Concept: Area of Two- Dimensional Figures | Concept: <br> Similarity | Concept: |
| :---: | :---: | :---: | :---: |
| $\sqrt{7}$ |  |  | $\checkmark$ |
| Lesson Essential Question/s: <br> How do you find the circumference of a circle? <br> How do find the area of a circle? | Lesson Essential Question/s: <br> How do you find the area of a twodimensional figures? <br> How do you find the area of composite figures? | Lesson Essential Question/s: <br> How are corresponding sides and corresponding angles related in similar figures? <br> How do you find missing measurements in similar figures? <br> How do you solve problems involving scale drawings? | Lesson Essential Question/s: |
| $\square$ |  |  |  |
| Vocabulary: <br> - Circle <br> - Circumference <br> - Diameter <br> - Radius <br> - Regular Polygon | Vocabularv: <br> - Edge <br> - Base <br> - Height <br> - Irregular Polygon <br> - Leg | Vocabulary: <br> - Scale Drawing <br> - Scale Factor <br> - Similar | Vocabulary: |

Course/Subject: $7^{\text {th }}$ Grade Math Length of instruction: 10 Days
Unit 8 Surface Area

## Unit Essential Ouestions:

How do you find the area of plane geometric figures?

How are similar figures and scale drawings related?

| Concept: <br> Circles | Concept: <br> Area of TwoDimensional Figures | Concept: <br> Similarity | Concept: |
| :---: | :---: | :---: | :---: |
| $\sqrt{5}$ |  |  | 5 |
| Lesson Essential Question/s: <br> How do you find the circumference of a circle? <br> How do find the area of a circle? | Lesson Essential Question/s: <br> How do you find the area of a twodimensional figures? <br> How do you find the area of composite figures? | Lesson Essential Question/s: <br> How are corresponding sides and corresponding angles related in similar figures? <br> How do you find missing measurements in similar figures? <br> How do you solve problems involving scale drawings? | Lesson Essential Question/s: |
| $\square$ |  | 7 | $\square$ |
| Vocabulary: <br> - Circle <br> - Circumference <br> - Diameter <br> - Radius <br> - Regular Polygon | Vocabulary: <br> - Edge <br> - Base <br> - Height <br> - Irregular Polygon <br> - Leg | Vocabulary: <br> - Scale Drawing <br> - Scale Factor <br> - Similar | Vocabulary: |

Topic: Unit 9: Volume
Days: 10
Subject(s): $7^{\text {th }}$ Grade Math

| Know: | Understand: |  |
| :--- | :--- | :--- |
| Cube | Understand how to <br> solve real-world <br> mathematical <br> problems involving <br> area, volume, and <br> surface area of two- <br> and three-dimensional <br> objects composted of <br> triangles, <br> quadrilaterals, <br> polygons, cubes, and <br> right prisms. | M07.C-G.2.2.2 Solve real-world and <br> mathematical problems involving area, <br> volume, and surface area of two- and three- <br> dimensional objects composed of triangles, <br> quadrilaterals, polygons, cubes, and right <br> prisms. |
| Net |  |  |
| Prism |  |  |
| Pyramid |  |  |
| Rectangular Prism |  |  |
| Rogular Polygon |  |  |

Unit 9 Volume

| Unit Essential Ouestions: |
| :---: |
| How do you find volume? |


| Concept: <br> Cross-Sections | Concept: <br> Volume | Concept: | Concept: |
| :---: | :---: | :---: | :---: |
| $\square$ |  | $\square$ | $\square$ |
| Lesson Essential Question/s: <br> How do you find the area of a cross-section? | Lesson Essential Question/s: <br> How do you find the volume of threedimensional figures? <br> How do you solve problems involving volume? | $\frac{\text { Lesson Essential }}{\text { Question/s: }}$ | Lesson Essential Question/s: |
|  |  | $\square$ | $\square$ |
| Vocabulary: <br> - Cube <br> - Cross Section <br> - Prism <br> - Pyramid <br> - Rectangular Prism <br> - Regular Polygon | Vocabulary: <br> - | Vocabulary: | Vocabulary: |

Topic: Unit 10: Data and Statistics
Subject(s): $7^{\text {th }}$ Grade Math

Days: 10
Grade(s): $7^{\text {th }}$

| Know: | Understand: | Do: |
| :---: | :---: | :---: |
| Biased Sample <br> Box plot <br> Dot plot <br> Interquartile Range <br> Median <br> Mean <br> Mean Absolute Deviation <br> Measures of Center <br> Measures of Variability <br> Population <br> Outlier <br> Quartile <br> Range <br> Sample <br> Spread <br> Survey <br> Unbiased Sample | Understand that statistics can be used to gain information about a population by examining a sample of the population. <br> Understand how to use data from a random sample to draw inferences about a population with an unknown characteristic of interest. <br> Understand how to use measures of center and measures of variability for numerical data from random samples to draw informal comparative inferences about two populations. | M07.D-S.1.1.1 Determine whether a sample is a random sample given a real-world situation. <br> M07.D-S.1.1.2 Use data from a random sample to draw inferences about a population with an unknown characteristic of interest. <br> M07.D-S.2.1.1 Compare two numerical data distributions using measures of center and variability. |

Course/Subject: $7^{\text {th }}$ Grade Math Length of instruction: 10 Days
Unit 10 Data and Statistics

| Unit Essential Ouestions: |
| :---: |
| How do you compare data? |



|  | $\bullet$ Outlier |  |  |
| :--- | :--- | :--- | :--- |
|  | $\bullet$ Quartile |  |  |
|  | $\bullet$ Range |  |  |
|  | $\bullet$ Spread |  |  |

Topic: Unit 11: Probability
Subject(s): $7^{\text {th }}$ Grade Math

Days: 10
Grade(s): $7^{\text {th }}$

| Know: | Understand: | Do: |
| :---: | :---: | :---: |
| Complementary Events <br> Compound Evets <br> Dependent Events <br> Independent Events <br> Experimental Probability <br> Theoretical Probability <br> Outcome <br> Probability <br> Random Event <br> Relative Frequency <br> Sample Space <br> Simple Event | Understand that the probability of a chance event is a number between 0 and 1 that expresses the likelihood of the event occurring. <br> Understand how to approximate the probability of a chance event by collecting data on the chance process that produces it and observing its long-run relative frequency and predict the approximate relative frequency given the probability. <br> Understand how to find the probabilities of compound events using organized lists, tables, tree diagrams, and simulation. | M07.D-S.3.1.1 Predict or determine whether some outcomes are certain, more likely, less likely, equally likely, or impossible. <br> M07.D-3.2.1 Determine the probability of a chance event given relative frequency and predict the approximate relative frequency given the probability. <br> M07.D-3.2.2 Find the probability of a simple event, including the probability of a simple event not occurring. <br> M07.D-S.3.2.3 Find probabilities of independent compound events using organized lists, tables, tree diagrams, and simulation. |

Course/Subject: $7^{\text {th }}$ Grade Math Length of instruction: 10 Days
Unit 11 Probability

## Unit Essential Ouestions:

How do you find probability?

| Concept: <br> Simple Probability | Concept: <br> Compound Probability | Concept: | Concept: |
| :---: | :---: | :---: | :---: |
| $\square$ | $\square$ | $\square$ | 5 |
| Lesson Essential Question/s: <br> How do you find the probability of a simple event? <br> How do you find the sample space of an event? <br> How are experimental and theoretical probability related? <br> How can probability help make predications? | Lesson Essential Question/s: <br> How do you find the probability of independent events? <br> How do you find the probability of dependent events? | Lesson Essential Question/s: | Lesson Essential Question/s: |
| $\square$ |  |  |  |
| Vocabulary: <br> - Complementary Events <br> - Experimental Probability <br> - Theoretical Probability <br> - Outcome <br> - Probability <br> - Random Event <br> - Relative Frequency | Vocabulary: <br> - Compound Evets <br> - Dependent Events <br> - Independent Events | Vocabulary: | Vocabulary: |


| $\bullet$ | Sample Space |  |  |
| :--- | :--- | :--- | :--- |
| $\bullet$ •Simple Event |  |  |  |

