

Course Title: Honors Precalculus

Board Approval Date:

Credit / Hours: 1 Credit

Reviewed Annually

Course Description:

This course provides students with a comprehensive study of the definitions, concepts, applications, and graphs of trigonometric, polynomial, rational, exponential, and logarithmic functions. The course is taught at an accelerated pace so that additional mathematical topics can be studied. These additional concepts include: sequences & series, factorials, and conic sections.

*Students will need a TI-89 graphing calculator for this course.

Learning Activities / Modes of Assessment:

Large group instruction

Experiments

Small group/team work

Journals/Learning Logs

Tests and Quizzes

Teacher Observation

Projects with Rubrics

Instructional Resources:

Precalculus with Limits/A Graphing Approach: Brooks/Cole CENGAGE Learning (2012,2008)

Course Pacing Guide

Course: Honors Precalculus

| Course Unit (Topic) (Days/Periods) | Length of Instruction |
|---|------------------------------|
| 1. Review of Linear Functions. | 20 days |
| 2. Polynomial Functions of Higher Degree | 25 days |
| 3. Rational Functions | 15 days |
| 4. Exponential and Logarithmic Functions. | 30 days |
| 5. Trigonometric Functions and their graphs | 45 days |
| 6. Analytic Trigonometry | 15 days |
| 7. Trigonometric Applications | 10 days |
| 8. Conic Sections | <u>20 days</u> |
| Total Days | 180 days |

Topic: 1 Review of Linear Functions

Days: 20

Subject(s): Math

Grade(s): 10th ,

| Know: | Understand: | Do: |
|---|-------------|--|
| <p>Review of identifying types of lines and linear functions</p> <p>Review of characteristics of functions</p> <p>Review of composition and inverse functions</p> | | <p>CC.2.2.HS.D.2 Write expressions in equivalent forms to solve problems.</p> <p>CC.2.2. HS.D.9 Use reasoning to solve equations and justify the solution method.</p> <p>CC.2.2.HS.D.10 Represent, solve, and interpret equations/inequalities and systems of equations/inequalities algebraically and graphically.</p> <p>CC.2.2.HS.C.1 Use the concept and notation of functions to interpret and apply them in terms of their context.</p> <p>CC.2.2.HS.C.2 Graph and analyze functions and use their properties to make connections between the different representations.</p> <p>CC.2.2.HS.C.3 Write functions or sequences that model relationships between two quantities.</p> <p>CC.2.2.HS.C.4 Interpret the effects transformations have on functions and find the inverses of functions.</p> <p>CC.2.2.HS.C.5 Construct and compare linear, quadratic, and exponential models to solve problems.</p> <p>CC.2.2.HS.C.6 Interpret functions in terms of the situations they model.</p> |

Topic: 1 Review of Linear Functions

Days: 20

Subject(s): Math

Key Learning: **Functions and their representations in the Cartesian Plane**



Unit Essential Question(s):

What are the main characteristics and components of linear functions and how are they used to model real-life problems?



Concept:

Lines in the Cartesian Plane

Concept:

Review of Functions

Concept:

Shifting, Reflecting, and Stretching Graphs



Lesson Essential Question(s):

How do you find the slope of a line and use it to write an equation of the line? (A)

Lesson Essential Question(s):

What are the important defining characteristics and representations of a function? (A)

How is the graph of a function used to determine the key elements of that function? (A)

Lesson Essential Question(s):

How do you write equations and draw graphs for the simple transformations of functions? (A)



Vocabulary:

Vocabulary:

Vocabulary:

Concept:

Combinations of Functions

Concept:

Inverse Functions

Concept:

Linear Models and Scatterplots



Lesson Essential Question(s):

How do you combine two functions to form a new function? (A)

Lesson Essential Question(s):

What is the inverse of a function and how do you represent it graphically and algebraically? (A)

Lesson Essential Question(s):

How do you write equations to model real-world data? (A)



Vocabulary:

Vocabulary:

Vocabulary:

Topic: 2 Polynomial Functions of higher degree

Days: 25

Subject(s): Math

Grade(s): 10th

| Know: | Understand: | Do: |
|---|---|--|
| <p>Use transformations to sketch polynomials graphs of polynomial functions</p> <p>Find and use zeros of polynomial functions as sketching aids.</p> <p>Analyze graphs of quadratic functions</p> <p>Write quadratic functions in standard form</p> <p>Find the minimum and maximum values of quadratic functions in real-life applications</p> | <p>How to graph polynomial Functions</p> <p>How to find the zeros of a polynomial equations</p> | <p>CC.2.2.HS.D.3 Extend the knowledge of arithmetic operations and apply to polynomials</p> <p>CC.2.2.HS.D. 4 Understand the relationship between zeros and factors of polynomials to make generalizations about functions and their graphs.</p> <p>CC.2.2.HS.D.5 Use polynomial identities to solve problems.</p> <p>CC.2.2.HS.D.8 Apply inverse operations to solve equations or formulas for a given variable.</p> <p>CC.2.2.HS.D.9 Use reasoning to solve equations and justify the solution method.</p> <p>CC.2.2.HS.D.10 Represent, solve, and interpret equations/inequalities and systems of equations/inequalities algebraically and graphically.</p> <p>CC.2.2.HS.C.1 Use the concept and notation of functions to interpret and apply them in terms of their context.</p> <p>CC.2.2.HS.C.2 Graph and analyze functions and use their properties to make connections between the different representations.</p> <p>CC.2.2.HS.C.3 Write functions or sequences that model relationships between two quantities</p> <p>CC.2.2.HS.C.5 Construct and compare linear, quadratic, and exponential models to solve problems.</p> <p>CC. 2.2.HS.C.6 Interpret functions in terms of the situations they model.</p> |

Topic: 2 Polynomial Functions of higher degree

Days: 25

Subject(s): Math

Key Learning: **Analyzing and Graphing polynomial functions**

Unit Essential Question(s):

**How are polynomial functions used to represent
real life applications?**



Concept:

Graphing polynomial functions of higher degree

Concept:

Applications of polynomial functions

Lesson Essential Question(s):

How do we sketch polynomial functions? (A)

How do we find the REAL zeros of a nonfactorable polynomial function? (A)

How do we write the equations of a polynomial function from characteristics and/or a sketch of the function? (A)

Lesson Essential Question(s):

How are polynomial functions used to model real life applications? (A)

Vocabulary:

zeros, fundamental theorem of algebra, rational root theorem

Vocabulary:

Topic: 3 Rational Functions

Days: 15

Subject(s): Math

Grade(s): 10th


| Know: | Understand: | Do: |
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| <p>Graph Rational Functions</p> <p>Finding the domain, discontinuities, and asymptotes</p> <p>Use rational functions to model and solve real life problems</p> | <p>How to find asymptotes and other discontinuities of rational graphs</p> <p>How to determine Domain and Range of rational functions</p> | <p>CC.2.2.HS.D.2 Write expressions in equivalent forms to solve problems.</p> <p>CC.2.2.HS.D.3 Extend the knowledge of arithmetic operations and apply to polynomials.</p> <p>CC.2.2.HS.D.4 Understand the relationship between zeros and factors of polynomials to make generalizations about functions and their graphs.</p> <p>CC.2.2.HS.D.5 Use polynomial identities to solve problems.</p> <p>CC.2.2.HS.D.6 Extend the knowledge of rational functions to rewrite in equivalent forms.</p> <p>CC.2.2.HS.D.7 Create and graph equations or inequalities to describe numbers or relationships.</p> <p>CC.2.2.HS.D.8 Apply inverse operations to solve equations or formulas for a given variable.</p> <p>CC.2.2.HS.D.9 Use reasoning to solve equations and justify the solution method.</p> <p>CC.2.2. HS.C.2 Graph and analyze functions and use their properties to take connections between the different representations.</p> <p>CC.2.2.HS.C.4 Interpret the effects transformations hoe on functions and find the inverses of functions.</p> <p>CC.2.2.HS.C.6 Interpret functions in terms of the situations they model.</p> |

Topic: 3 Rational Functions

Days: 15

Subject(s): Math

Key Learning:
How to find asymptotes and other discontinuities of rational functions
How to determine Domain and Range of rational functions



Unit Essential Question(s): How do I graph rational functions and use them model real life problems?

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| <p>Concept: Graphing rational functions</p> | <p>Concept: Real Life Applications</p> | <p>Concept: Domain and asymptotes of rational functions</p> |
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| <p>Lesson Essential Question(s): <u>What do we identify the domains and asymptotes of graphs of rational functions? (A)</u> What are the basic characteristics of a Rational Function? (A)</p> | <p>Lesson Essential Question(s): How do we use rational functions to model real life problems? (A)</p> | <p>Lesson Essential Question(s): What do we identify the domains and asymptotes of graphs of rational functions? (A)</p> |
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| <p>Vocabulary:</p> | <p>Vocabulary:</p> | <p>Vocabulary:</p> |
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Topic: 4 Exponential & Logarithmic Functions

Days: 30

Subject(s): Math

Grade(s): 10th

| Know: | Understand: | Do: |
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| Graphs of exponential functions | To graph an exponential function | CC.2.2.HS.D.2 Write expressions in equivalent forms to solve problems. |
| Properties of exponentials | To interpret the key characteristics of the graphs of exponential functions | CC.2.2.HS.D.8 Apply inverse operations to solve equations or formulas for a given variable |
| Asymptote | | CC.2.2.HS.D.9 Use reasoning to solve equations and justify the solution method. |
| Inverses | To use the properties of exponents to solve exponential equations | |
| Properties of Logarithms | | CC.2.2.HS.D.10 Represent, solve, and interpret equations/inequalities and systems of equations/inequalities algebraically and graphically. |
| Logarithmic equations | To use the properties of logarithms to solve exponential and logarithmic equations | CC.2.2.HS.C.2 Graph and analyze functions and use their properties to make connections between the different representations. |
| Definition of a logarithm | | |
| Graphing Logarithmic Functions | To evaluate logarithms | CC.2.2.HS.C.3 Write functions or sequences that model relationships between two quantities. |
| Applications of Exponential and Logarithmic Functions | To solve applications of exponential and logarithmic functions | CC.2.2.HS.C.4 Interpret the effects transformations have on functions and find the inverses of functions. |
| | | CC.2.2.HS.C.5 Construct and compare linear, quadratic, and exponential models to solve problems. |
| | | CC.2.2.HS.C.6 Interpret functions in terms of the situations they model. |

Topic: 4 Exponential & Logarithmic Functions
 Subject(s): Math

Days: 15

Key Learning:

What are the characteristics of the graph of an exponential function?

What are the characteristics of the graph of an logarithmic function?

What are the areas of application for both types of functions?



Unit Essential Question(s):

How do we use exponential and logarithmic functions to model real life application problems?

Concept:

Review Graphing of Exponential Functions

Concept:

Graphing Logarithmic Functions

Concept:

Applications of Exponential and Logarithmic Functions

Lesson Essential Question(s):

What are the basic characteristics of an exponential function? (A)

Lesson Essential Question(s):

what are the basic characteristics of a logarithmic function? (A)

How are exponential and logarithmic functions related? (A)

Lesson Essential Question(s):

What are the five most common models involving exponential or logarithmic functions? (A)

Vocabulary:

Vocabulary:

Vocabulary:

Concept:

Solving Exponential and logarithmic equations

Lesson Essential Question(s):

How do we solve exponential and logarithmic equations? (A)

How do we use the properties of logarithms to solve logarithmic equations. (A)

Vocabulary:

Topic: 5 Trigonometric Functions
and their graphs

Days: 45

Grade(s): 10th

Subject(s): Math

| Know: | Understand: | Do: |
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| <p>Definitions of the 6 trigonometric functions</p> <p>Graph of the 6 trigonometric functions</p> <p>Radian measure</p> <p>Inverse trigonometric functions</p> | <p>Measuring angles in degrees and radians.</p> <p>Interpreting the graphs of the 6 trigonometric functions</p> <p>Evaluating the six trigonometric functions</p> <p>Evaluating inverse trigonometric functions</p> | <p>CC.2.2.HS.C.1 Use the concept and notation of functions to interpret and apply them in terms of their context.</p> <p>CC.2.2.HS.C.2 Graph and analyze functions and use their properties to make connections between the different representations.</p> <p>CC.2.2.HS.C.3 Write functions or sequences that model relationships between two quantities.</p> <p>CC.2.2.HS.C.4 Interpret the effects transformations have on functions and find the inverses of functions.</p> <p>CC.2.2.HS.C.7 Apply radian measure of an angle and the unit circle to analyze the trigonometric functions.</p> <p>CC.2.2.HS.C.9 Prove the Pythagorean identity and use it to calculate trigonometric ratios.</p> |

Topic: Unit 5 Trigonometric functions and their graphs.

Unit Essential Question:

What are the properties of trigonometric functions and their graphs?

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| <p><u>Concept:</u></p> <p>Radians, Degrees and the Unit Circle</p> | <p><u>Concept:</u></p> <p>How do we evaluate the six trigonometric functions?</p> | <p><u>Concept:</u></p> <p>Graphing Trigonometric Functions and their inverses.</p> |
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| <p><u>Lesson Essential Question/s:</u></p> <p>How do you describe angles and angular movement? (A)</p> <p>How do you use the arc length formula to find angular velocity and linear velocity? (A)</p> | <p><u>Lesson Essential Question/s:</u></p> <p>How do we find the exact values of the six trigonometric functions given a point on the terminal side of the angle? (A)</p> <p>How do we find the six trigonometric functions given the measure of an angle in degrees or radians?</p> | <p><u>Lesson Essential Question/s:</u></p> <p>How do you sketch the graphs of the six trigonometric functions? (A)</p> <p>What are the characteristics of the inverse trigonometric function and their graphs? (A)</p> <p>How do we identify the characteristics of a trigonometric function including the domain, range and asymptotes? (A)</p> <p>How do we evaluate inverse trigonometric expressions? (A)</p> |
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| <p><u>Vocabulary:</u></p> <p>Radians, Angular Velocity, Linear Velocity, Arc Length, Coterminal, Initial ray, Terminal ray</p> | <p><u>Vocabulary:</u></p> <p>Sine, Cosine, Tangent, Secant, Cosecant, Cotangent.</p> | <p><u>Vocabulary:</u></p> <p>Inverse, Domain, Range, Vertical Line Test, Horizontal Line Test.</p> |
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Topic: 6 Analytic Trigonometry

Subject(s): Math

| Know: | Understand: | Do: |
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| <p>Fundamental Trigonometric Identities</p> <p>Verification of Identities</p> <p>Sum and Difference Formulas</p> | <p>Solving trigonometric equations using identities</p> <p>Proving and Verifying trigonometric identities</p> <p>Using Sum and Difference Formulas</p> | <p>CC.2.2.HS.C.3 Write functions or sequences that model relationships between two quantities.</p> <p>CC.2.2.HS.C.4 Interpret the effects transformations have on functions and find the inverses of functions.</p> <p>CC.2.2.HS.C.7 Apply radian measure of an angle and the unit circle to analyze the trigonometric functions.</p> <p>CC.2.2.HS.C.8 Choose trigonometric functions to model periodic phenomena and describe the properties of the graphs.</p> <p>CC.2.2.HS.C.9 Prove the Pythagorean identity and use it to calculate trigonometric ratios.</p> |

Topic: Unit 6 Analytic Trigonometry

Unit Essential Question:

How do we use the trigonometric identities to solve equations and prove or verify trigonometric identities?

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| <p><u>Concept:</u></p> <p>Solving Trigonometric equations</p> | <p><u>Concept:</u></p> <p>Verifying and proving trigonometric identities</p> |
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| <p><u>Lesson Essential Question/s:</u></p> <p>How do you solve trigonometric equations written in quadratic form or containing more than one angle? (A)</p> <p>How do you simplify expressions and solve equations that contain sums or differences of angles? (A)</p> <p>How do you rewrite trigonometric expressions that contain functions of multiple or half angles or functions that involve squares or products of trigonometric expressions? (A)</p> | <p><u>Lesson Essential Question/s:</u></p> <p>How do we verify the basic trigonometric identities? (A)</p> <p>How do we use the fundamental identities to prove other trigonometric identities? (A)</p> |
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| <p><u>Vocabulary:</u></p> <p>Trigonometric half angles and multiple angles. hippopotomonstrosesquippedaliophobia</p> | <p><u>Vocabulary:</u></p> <p>Sine, Cosine, Tangent, Secant, Cosecant, Cotangent.</p> |
|---|---|

Topic: 7 Trigonometric Applications
 Subject(s): Math

Days: 10
 Grade(s): 10th

| Know: | Understand: | Do: |
|---|---|---|
| <p>Arclength and Area of a sector</p> <p>Law of Sines</p> <p>Law of Cosines</p> <p>Heron's Formula</p> <p>Area of Triangles</p> <p>Real life applications</p> | <p>To solve triangles</p> <p>To find the area of triangles</p> <p>Solve trigonometric equations using identities</p> <p>Applications and Modeling</p> | <p>CC.2.2.HS.C.1 Use the concept and notation of functions to interpret and apply them in terms of their context.</p> <p>CC.2.2.HS.C.2 Graph and analyze functions and use their properties to make connections between the different representations.</p> <p>CC.2.2.HS.C.3 Write functions or sequences that model relationships between two quantities.</p> <p>CC.2.2.HS.C.6 Interpret functions in terms of the situations they model.</p> <p>CC.2.2.HS.C.8 Choose trigonometric functions to model periodic phenomena and describe the properties of the graphs</p> <p>CC.2.2.HS.D.2 Write expressions in equivalent forms to solve problems.</p> |

Topic: Unit 7 Trigonometric applications

Unit Essential Question:
How do we use the trigonometric functions to solve real life application problems?

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| <u>Concept:</u> Applications of Trigonometric Functions | <u>Concept:</u> Fitting Trigonometric Models to data using a graphing utility. |
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| <u>Lesson Essential Question/s:</u> What are the real life problems involving right triangles? (A) How do I solve problems involving harmonic motions? (A) How do we use trigonometry to solve problems involving directional bearings? (A) | <u>Lesson Essential Question/s:</u> How do we use a regression curve to fit a data set using a Sine Regression on a graphing utility? (A) |
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| <u>Vocabulary:</u> Angle of elevation, angle of depression. Nautical miles. | <u>Vocabulary:</u> Regression |
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**Topic: 8 Analytic Geometry-
Conic Sections**

Subject(s): Math

| Know: | Understand: | Do: |
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| <p>The equations of Circles and Parabolas</p> <p>Ellipses</p> <p>Hyperbolas and Rotations of Conic Sections</p> | <p>Recognizing Conic Sections</p> <p>Solving Problems involving parabolas</p> <p>Solving Problems involving ellipses</p> <p>Solving Problems involving hyperbolas</p> <p>Classifying a conic section from its general equation</p> | <p>CC.2.2.HS.C.1 Use the concept and notation of functions to interpret and apply them in terms of their context.</p> <p>CC.2.2.HS.C.2 Graph and analyze functions and use their properties to make connections between the different representations.</p> <p>CC.2.2.HS.C.4 Interpret the effects transformations have on functions and find the inverses of functions.</p> <p>CC.2.2.HS.C.7 Apply radian measure of an angle and the unit circle to analyze the trigonometric functions.</p> <p>CC.2.2.HS.C.9 Prove the Pythagorean identity and use it to calculate trigonometric ratios.</p> |

Topic: Unit 8 Conic Sections

Unit Essential Question:
What are the graphs created by the intersection of a plane and a cone or pair of cones?

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| <u>Concept:</u> Equations of Conic Sections | <u>Concept:</u> Graphs of Conic Sections |
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| <u>Lesson Essential Question/s:</u> How do we determine the equation of conic section? (A) What is the importance of the foci and how do we find them? (A) | <u>Lesson Essential Question/s:</u> How do we graph conic sections? (A) How do we determine the type of graph we should expect based on the equation of the function? (A) How do we write the equation of the function based on the graph? (A) |
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| <u>Vocabulary:</u> Circle, Ellipse, Hyperbola, Parabola | <u>Vocabulary:</u> Foci, focus, major axis, minor axis. |
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